

Multi-Stream Opportunistic Network Decoupling: Relay Selection and Interference Management

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Abstract—We study multi-stream transmission in the $K \times N \times K$ channel with *interfering relay nodes*, consisting of K *multi-antenna* source–destination (S–D) pairs and N single-antenna half-duplex relay nodes between the S–D pairs. We propose a new achievable scheme operating with partial effective channel *gain*, termed *multi-stream opportunistic network decoupling (MS-OND)*, which achieves the optimal degrees of freedom (DoF) under a certain relay scaling law. Our protocol is built upon the conventional OND that leads to *virtual full-duplex* mode with one data stream transmission per S–D pair, generalizing the idea of OND to multi-stream scenarios by leveraging relay selection and interference management. Specifically, two subsets of relay nodes are opportunistically selected using alternate relaying in terms of producing or receiving the minimum total interference level. For interference management, each source node sends S ($1 \leq S \leq M$) data streams to selected relay nodes with *random beamforming* for the first hop, while each destination node receives its desired S streams from the selected relay nodes via *opportunistic interference alignment* for the second hop, where M is the number of antennas at each source or destination node. Our analytical results are validated by numerical evaluation.

Index Terms—Degree of freedom (DoF), $K \times N \times K$ channel, multi-stream opportunistic network decoupling (MS-OND), opportunistic interference alignment (OIA), random beamforming (RBF), virtual full-duplex

1 INTRODUCTION

INTERNET of Things (IoT) has been emerging as a promising technology that integrates the physical world into computer-based systems [1]. Recent developments of the IoT have also spurred research and standardization efforts on massive machine type communications (mMTC) in the fifth generation (5G) wireless networks [2]. In such wireless networks, a massive number of devices with low energy and low cost can be deployed, e.g., connection density of 1×10^6 devices per km^2 in urban areas may be necessary [3], where the half-duplex and single-antenna configuration is preferable [4]. Thus, it would be important to design an effective protocol that guarantees satisfactory performance even under such low-cost requirements on the devices.

1.1 Previous Work

Interference management has been taken into account as one of the most challenging and important issues in wireless multiuser communications [5]. While it has been elusive to characterize the Shannon-theoretic capacity of interference

channels, interference alignment (IA) was proposed for fundamentally solving the interference problem among multiple communication pairs [6], [7]. It was shown that the IA scheme in [7] can achieve the optimal degrees of freedom (DoF), which is equal to $K/2$, in the K -user interference channel with time-varying channel coefficients. Interference management schemes based on IA have been further developed and analyzed in various wireless network environments such as multiple-input multiple-output (MIMO) interference networks [8], [9], X networks [10], and cellular networks [11], [12], [13], [14], [15], [16].

Recently, the K -user *two-hop relay-aided* interference channel (also known as the $K \times N \times K$ channel), which consists of K source–destination (S–D) pairs and N helping relay nodes located between the S–D pairs, has received a great deal of attention from academia [17], [18], [19]. The $K \times N \times K$ channel is more challenging than the K -user interference channel because interference management and cooperative relaying operations that are coupled with each other need to be carefully conducted. In the $2 \times 2 \times 2$ interference channel, as a special case of the $K \times N \times K$ channel, it was shown that interference neutralization achieves the optimal DoF [17]. In addition, aligned network diagonalization was proposed for the general $K \times N \times K$ channel to achieve the optimal DoF [18]. However, it was assumed in [17], [18], [19] that relay nodes are full-duplex and/or there is no interfering signal among relay nodes.

On the other hand, there have been extensive studies on how to exploit the *multiuser diversity* gain in single-cell downlink scenarios when the number of users is sufficiently large by introducing opportunistic scheduling [20], opportunistic beamforming [21], and random beamforming (RBF)

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[22]. For multi-cell downlink scenarios, multi-cell RBF schemes were proposed in [23], [24]. Moreover, a joint design of IA-enabled beamforming and opportunistic scheduling, called *opportunistic interference alignment (OIA)*, has been proposed in multi-cell uplink or downlink networks [13], [14], [15], [16]. Even without centralized controlling, the benefits of opportunistic transmission were also examined in slotted ALOHA-based random access networks [25], [26], [27], [28]. By applying opportunism to cooperative communications, various techniques such as opportunistic two-hop relaying [29], [30] and opportunistic routing [31], [32], [33] were investigated. As for the $K \times N \times K$ channel having *interfering relay nodes*, *opportunistic network decoupling (OND)* was recently proposed while showing that K DoF is asymptotically achieved even in the presence of inter-relay interference when N is beyond a certain value [34]. In the OND protocol, two sets of relay nodes are selected among total N relay candidates to alternatively receive signals from source nodes or forward signals to destination nodes in each time slot, thus realizing the virtual full-duplex mode. The two relay sets are opportunistically selected in the sense that both the interference among S-D pairs and the interference among relay nodes are effectively controlled. The OND protocol in [34] would be feasible in practice due to the fact that not only it effectively manages the inter-relay interference unlike the studies in [17], [18], [19] but also the network operates in virtual full-duplex mode even with half-duplex relay nodes.

Meanwhile, to deal with self-interference that is generally far stronger than the signal of interest in full-duplex systems [35], several self-interference cancellation (SIC) techniques have been developed. Examples include the sum-rate optimization for full-duplex multi-antenna relaying systems under limited dynamic range [36], [37].

1.2 Main Contributions

The prior work in [34] basically deals with single-stream transmission for each S-D pair since a single antenna is assumed to be deployed at each source and destination node. With the increasing number of antennas at mobile terminals in wireless communication systems, a natural question arises as follows: how can one successfully deliver multiple data streams for each *multi-antenna* S-D pair by fully exploiting the multiuser diversity gain in fading channels? We attempt to answer this fundamental question in this paper. As an extension of the single-antenna configuration in [18], [34], we consider the multi-antenna $K \times N \times K$ channel with N single-antenna interfering *half-duplex* relay nodes operating in time-division duplex (TDD) mode, where each of K source and destination nodes is equipped with M antennas and each source node sends S ($1 \leq S \leq M$) data streams. Extension to the *multi-stream* scenario is not straightforward since more challenging and sophisticated interference management and relay selection strategies are accompanied under the channel model. In particular, we need to elaborately handle the inter-stream interference among multiple spatial streams in each S-D pair, in addition to the inter-pair interference and inter-relay interference that have appeared in the single-antenna $K \times N \times K$ channel [34].

In this paper, we propose a *multi-stream OND (MS-OND)* protocol operating in a fully distributed manner only with

partial effective channel *gain* information at the transmitters. Typical application scenarios of the proposed MS-OND protocol include mMTC and IoT in the 5G wireless networks, where a massive number of low-cost devices with the *half-duplex and single-antenna configuration* can be deployed, providing potentially strong supports as candidate relay nodes [4]. Based upon the single-stream OND protocol in [34], MS-OND is designed by further leveraging both interference management and relay selection techniques. To be specific, two subsets of relay nodes among N relay candidates are opportunistically selected while *alternate relaying* is used in terms of generating or receiving the minimum total interference level (TIL), which eventually enables our system to operate in *virtual full-duplex* mode. Furthermore, for interference management, our protocol intelligently integrates RBF for the first hop and OIA for the second hop into the comprehensive network decoupling framework. Such a protocol integration is a challenging task since it involves various techniques across different domains such as scheduling, beamforming, and interference management. As our main result, it is shown that in a high signal-to-noise ratio (SNR) regime, the proposed MS-OND protocol achieves SK DoF provided that the number of relay nodes, N , scales faster than $\text{SNR}^{3SK-S-1}$, which is the minimum number of relay nodes required to guarantee the DoF achievability.

Our main contributions are fourfold and summarized as follows:

- For the multi-antenna $K \times N \times K$ channel with interfering relay nodes, we introduce a general OND framework, which enables each S-D pair to perform multi-stream communications by incorporating the notion of RBF and OIA techniques into the protocol design.
- Under the channel model, we completely analyze the achievable DoF under a certain relay scaling condition and the decaying rate of the TIL. Furthermore, the MS-OND protocol is shown to asymptotically approach the cut-set upper bound on the DoF.
- Our analytical results (i.e., the relay scaling law required to achieve a given DoF) are numerically validated through extensive computer simulations.
- We also perform extensive computer simulations in *finite* system parameter regimes to show when the MS-OND protocol with alternate relaying is prominent in practice.

1.3 Organizations

The rest of this paper is organized as follows. In Section 2, we describe the system and channel models. In Section 3, the proposed MS-OND protocol is described. Section 4 presents analysis on both the achievable DoF and the decaying rate of the TIL. Numerical results for the proposed MS-OND protocol are provided in Section 5. Finally, we summarize the paper with some concluding remarks in Section 6.

1.4 Notations

Throughout this paper, \mathbb{C} , $\mathbb{E}[\cdot]$, and $\lceil \cdot \rceil$ indicate the field of complex numbers, the statistical expectation, and the ceiling operation, respectively. Unless otherwise stated, all logarithms are assumed to be to the base 2. We use the following asymptotic notation: $f(x) = O(g(x))$ means that there exist

TABLE 1
Summary of Notations

Notation	Description
K	number of S-D pairs
N	number of relay nodes
M	number of antennas at each S-D pair
S	number of data streams per S-D pair
S_k	k th source node
\mathcal{D}_k	k th destination node
\mathcal{R}_n	n th relay node
$\mathbf{h}_{nk}^{(1)}$	channel coefficient vector from S_k to \mathcal{R}_n
$\mathbf{h}_{kn}^{(2)}$	channel coefficient vector from \mathcal{R}_n to \mathcal{D}_k
$h_{mn}^{(r)}$	channel coefficient between \mathcal{R}_n and \mathcal{R}_m
$\Pi_b (b = \{1, 2\})$	two selected relay sets
$L_{n,(k,s)}^{\Pi_1}$	scheduling metric of the first relay set Π_1
$L_{n,(k,s)}^{\Pi_2}$	scheduling metric of the second relay set Π_2
$\text{DoF}_{\text{total}}$	total number of DoF

constants C and c such that $f(x) \leq Cg(x)$ for all $x > c$; $f(x) = \Omega(g(x))$ if $g(x) = O(f(x))$; $f(x) = \omega(g(x))$ means that $\lim_{x \rightarrow \infty} \frac{g(x)}{f(x)} = 0$; and $f(x) = \Theta(g(x))$ if $f(x) = O(g(x))$ and $g(x) = O(f(x))$ [38]. Moreover, Table 1 summarizes the notations used throughout this paper. Some notations will be more precisely defined in the following sections, as we introduce our channel model and achievability results.

2 SYSTEM AND CHANNEL MODELS

We consider the multi-antenna $K \times N \times K$ channel with interfering relay nodes, where each source or destination node is equipped with M antennas while each relay node is equipped with a single antenna.¹ We assume that there exists no direct communication path between each S-D pair as the source and destination nodes are geographically far apart. Each source node sends S ($1 \leq S \leq M$) independent data streams to the corresponding destination node through $2S$ relay nodes. There are two relay sets composed of $2SK$ relay nodes, where each relay set is opportunistically selected out of N relay candidates (which will be specified in Section 3.2).² Each relay node is assumed to operate in half-duplex mode and to fully decode, re-encode, and retransmit the source data, i.e., to employ decode-and-forward (DF) relaying. The relay nodes are assumed to interfere with each other when sending data to the belonging destination nodes. We assume that each node (either a source node or a relay node) has an average transmit power constraint P .

Let S_k , \mathcal{D}_k , and \mathcal{R}_n denote the k th source node, the corresponding k th destination node, and the n th relay node, respectively, where $k \in \{1, 2, \dots, K\}$ and $n \in \{1, 2, \dots, N\}$. The channel coefficient vector from the source S_k to the relay \mathcal{R}_n , corresponding to the first hop, is denoted by $\mathbf{h}_{nk}^{(1)} \in \mathbb{C}^{M \times 1}$; the channel coefficient vector from the relay \mathcal{R}_n

to the destination \mathcal{D}_k , corresponding to the second hop, is denoted by $\mathbf{h}_{kn}^{(2)} \in \mathbb{C}^{1 \times M}$; and the channel coefficient between two relay nodes \mathcal{R}_n and \mathcal{R}_m is denoted by $h_{mn}^{(r)}$. All the channel coefficients are assumed to be Rayleigh, having zero-mean and unit variance, and to be independent independent and identically distributed (i.i.d.) over different k, n, m , and the hop index. We assume the block-fading model, i.e., the channels are constant during one block, consisting of one initialization phase and L data transmission time slots, and change to new independent values for every block. In our work, we assume that partial channel gain information (i.e., channel gains that can be estimated via pilot signaling) is only available at the transmitters.

3 PROPOSED MS-OND PROTOCOL

In this section, we elaborate on the MS-OND protocol as an achievable scheme that guarantees the optimal DoF for the multi-antenna $K \times N \times K$ channel with inter-relay interference, where $2SK$ relay nodes among N relay candidates are opportunistically selected for data reception and forwarding in the sense of generating or receiving a sufficiently small amount of interference. Furthermore, we describe two opportunistic transmission techniques including RBF for the first hop and OIA for the second hop that are intelligently integrated into our network decoupling framework.

3.1 Overall Procedure

For the sake of explanation, we assume that the number of data transmission time slots, L , is odd. The overall procedure of the MS-OND protocol is described as follows.

(a) *Initialization Phase.* The source nodes generate and broadcast RBF vectors for the first hop. More specifically, the source S_k generates M RBF vectors according to the isotropic distribution [39] that are constructed by an $M \times M$ unitary matrix $\mathbf{V}_k = [\mathbf{v}_k^{(1)}, \mathbf{v}_k^{(2)}, \dots, \mathbf{v}_k^{(M)}]$. Here, $\mathbf{v}_k^{(i)} \in \mathbb{C}^{M \times 1}$ is the i th RBF vector of the source S_k , where $i \in \{1, 2, \dots, M\}$. The destination nodes generate and broadcast their interference space so that OIA is employed for the second hop. More specifically, the destination \mathcal{D}_k generates the interference space denoted by $\mathbf{Q}_k = [\mathbf{q}_k^{(1)}, \dots, \mathbf{q}_k^{(M-S)}]$, where $\mathbf{q}_k^{(i)} \in \mathbb{C}^{M \times 1}$ is the orthonormal basis and $S \in \{1, 2, \dots, M\}$. The corresponding null space at the destination \mathcal{D}_k , indicating the signal space, is defined as $\mathbf{U}_k = [\mathbf{u}_k^{(1)}, \dots, \mathbf{u}_k^{(S)}] \triangleq \text{null}(\mathbf{Q}_k)$, where $\mathbf{u}_k^{(i)} \in \mathbb{C}^{M \times 1}$ is the orthonormal basis. For the space generation, we choose $M - S$ columns of the left or right singular matrix of any $M \times M$ matrix as \mathbf{Q}_k and choose the rest S columns as \mathbf{U}_k . If $S = M$, then \mathbf{U}_k can be any orthogonal matrix.

Two relay sets Π_1 and Π_2 among N relay candidates, each of which consists of SK relay nodes, are selected to alternately receive and forward SK independent data streams for K S-D pairs so that each S-D pair is assisted by $2S$ relay nodes. The relay sets Π_1 and Π_2 are denoted by

$$\Pi_1 = \{\pi_1(1, 1), \pi_1(1, 2), \dots, \pi_1(1, S), \dots, \pi_1(K, 1), \pi_1(K, 2), \dots, \pi_1(K, S)\},$$

and

$$\Pi_2 = \{\pi_2(1, 1), \pi_2(1, 2), \dots, \pi_2(1, S), \dots, \pi_2(K, 1), \pi_2(K, 2), \dots, \pi_2(K, S)\},$$

1. We do not assume to equip multiple antennas at each relay node since it does not further improve the DoF and may cause the space limitation as relay nodes are treated as small-size sensors.

2. As mentioned in Section 1.2, it is assumed to deploy a massive number of devices as potential relay nodes in mMTC or IoT wireless networks, which are the target application scenarios of our MS-OND protocol.

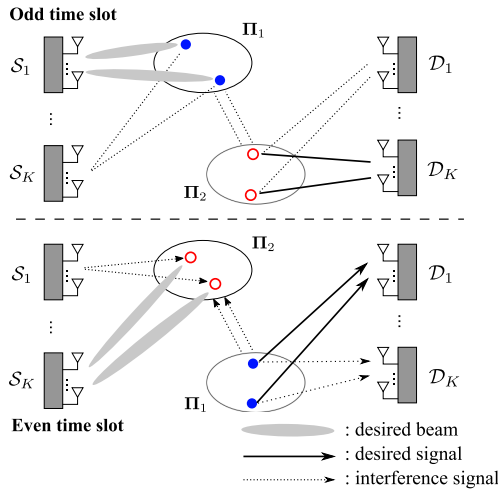


Fig. 1. Illustration of the MS-OND protocol operation in the $K \times N \times K$ channel with interfering relay nodes when each S–D pair equips multiple antennas.

respectively. Here, $\pi_b(k, s)$ denotes the index of the relay node who serves the s th data stream of the k th S–D pair in the relay set Π_b , where $b \in \{1, 2\}$, $k \in \{1, 2, \dots, K\}$, and $s \in \{1, 2, \dots, S\}$. The rest $N - 2SK$ relay nodes remain idle during all the time slots.

(b) *Odd Time Slot* $l_o \in \{1, 3, \dots, L\}$. As shown in Fig. 1, by virtue of RBF, each source node transmits its S encoded symbols along with S spatial beams to S relay nodes in the relay set Π_1 . For instance, the source S_k transmits symbols $x_{k,1}^{(1)}(l_o), \dots, x_{k,S}^{(1)}(l_o)$ on S spatial beams, where $k \in \{1, 2, \dots, K\}$. The relay $\mathcal{R}_{\pi_1(k,s)}$ receives the desired symbol $x_{k,s}^{(1)}(l_o)$ on the s th spatial beam of the source S_k , where $s \in \{1, 2, \dots, S\}$.³ Meanwhile, the relay nodes in the relay set Π_2 forward the symbols received from the source nodes in the previous time slot by using DF relaying at the same time. Note that in the first time slot (i.e., $l_o = 1$), the relay nodes in the relay set Π_2 remain idle since there is no symbol to forward. In the last time slot (i.e., $l_o = L$), the S–R transmission is not required, and thus all the source nodes and the relay nodes in the relay set Π_1 remain idle.

(c) *Even Time Slot* $l_e \in \{2, 4, \dots, L - 1\}$. The source S_k transmits S encoded symbols $x_{k,1}^{(2)}(l_e), \dots, x_{k,S}^{(2)}(l_e)$ to S relay nodes in the relay set Π_2 . The relay nodes in the relay set Π_1 forward their re-encoded symbols to the intended destination nodes at the same time. For instance, relay nodes $\mathcal{R}_{\pi_1(k,1)}, \dots, \mathcal{R}_{\pi_1(k,S)}$ transmit the symbols $x_{\pi_1(k,1)}^{(2)}(l_e - 1), \dots, x_{\pi_1(k,S)}^{(2)}(l_e - 1)$ to the destination \mathcal{D}_k while the interfering signals to other destination nodes are opportunistically aligned to the interference space of the destination nodes. If the relay $\mathcal{R}_{\pi_1(k,s)}$ in the relay set Π_1 successfully decodes its desired symbol, then $x_{\pi_1(k,s)}^{(2)}(l_e - 1)$ is the same as $x_{k,s}^{(1)}(l_e - 1)$.

(d) *Reception at the Destination Nodes*. The relay sets Π_1 and Π_2 alternately operate in receive and transmit modes in the odd and even time slots, respectively. The destination nodes operate in receive mode for all the time slots except the first time slot, while decoding the symbols forwarded by either the relay set Π_1 (in the even time slots) or the relay

set Π_2 (in the odd time slots) by adopting zero-forcing (ZF) detection.⁴ Note that for each destination node, the received interference from the relay nodes other than its own assisting relay nodes can be well confined by virtue of OIA for the second hop as the number of relay nodes is sufficiently large.

3.2 Relay Set Selection

In this section, we describe how to select the two relay sets Π_1 and Π_2 . By exploiting the multiuser diversity gain in fading channels, relay nodes are opportunistically selected in the sense of generating or receiving the minimum sum amount of the following three types of interference: i) interference from other spatial beams during the S–R transmission; ii) interference leakage to other destination nodes during the R–D transmission; and iii) interference between two relay sets.

3.2.1 The First Relay Set Selection

Let us first focus on selecting the relay set Π_1 from N relay candidates, which operates in receive and transmit modes in odd and even time slots, respectively. For every initialization period, it is possible for the relay \mathcal{R}_n to acquire a part of *effective channel gain* information via pilot signaling sent from all the source and destination nodes due to the channel reciprocity of TDD systems before data transmission, where $n \in \{1, 2, \dots, N\}$ and $k \in \{1, 2, \dots, K\}$ (which will be specified later). When the relay \mathcal{R}_n is assumed to serve the s th data stream of the k th S–D pair, it examines both i) how much interference is received from other spatial beams created by RBF for the first hop, including the interference from other source nodes and the interference from other $S - 1$ spatial beams of the source S_k ; and ii) how much interference leakage is generated by itself to other destination nodes via OIA for the second hop. Then, the relay \mathcal{R}_n computes the following scheduling metric $L_{n,(k,s)}^{\Pi_1}$:

$$L_{n,(k,s)}^{\Pi_1} = \sum_{\substack{t=1 \\ t \neq s}}^S \left| \mathbf{v}_k^{(t)T} \mathbf{h}_{nk}^{(1)} \right|^2 + \sum_{\substack{j=1 \\ j \neq k}}^K \sum_{t=1}^S \left| \mathbf{v}_j^{(t)T} \mathbf{h}_{nj}^{(1)} \right|^2 + \sum_{\substack{j=1 \\ j \neq k}}^K \left\| \text{Proj}_{\perp \mathbf{Q}_j} \left(\mathbf{h}_{jn}^{(2)} \right) \right\|^2, \quad (1)$$

where $n \in \{1, 2, \dots, N\}$, $k \in \{1, 2, \dots, K\}$, and $s \in \{1, 2, \dots, S\}$. Here, $\text{Proj}_{\perp \mathbf{Q}_j} \left(\mathbf{h}_{jn}^{(2)} \right) \triangleq \mathbf{U}_j^H \mathbf{h}_{jn}^{(2)}$ denotes the orthogonal projection of $\mathbf{h}_{jn}^{(2)}$ onto \mathbf{U}_j . Thus, the last term $\sum_{\substack{j=1 \\ j \neq k}}^K \left\| \text{Proj}_{\perp \mathbf{Q}_j} \left(\mathbf{h}_{jn}^{(2)} \right) \right\|^2$ in (1) indicates the sum of interference leakage links generated by the relay \mathcal{R}_n to other $K - 1$ destination nodes, which can also be estimated at each relay node as all the destination nodes send pilot signaling multiplied by their null space. In this selection stage, we aim to find the relay set Π_1 leading to negligibly small values of $L_{n,(k,s)}^{\Pi_1}$. We also remark that the first and second terms in (1), $\sum_{\substack{t=1 \\ t \neq s}}^S \left| \mathbf{v}_k^{(t)T} \mathbf{h}_{nk}^{(1)} \right|^2$ and $\sum_{\substack{j=1 \\ j \neq k}}^K \sum_{t=1}^S \left| \mathbf{v}_j^{(t)T} \mathbf{h}_{nj}^{(1)} \right|^2$, denote the sum of interference

4. It is worth noting that more sophisticated detection methods (e.g., minimum mean square error detection) can also be employed at the receivers since our MS-OND protocol is detector-agnostic. Even if employing a more sophisticated detection method could further improve the sum-rate performance of our MS-OND protocol, we adopt ZF detection, which is sufficient to achieve the optimal DoF.

3. Detailed data transmission process will be described in Section 3.3.

links from other spatial beams of the source \mathcal{S}_k and from other source nodes, respectively, which can be estimated at each relay node as all the source nodes send pilot signaling multiplied by their RBF vectors. Note that inter-relay interference cannot be computed when the relay set Π_1 is selected because neither Π_1 nor Π_2 is available in this phase and it is sufficient to consider the inter-relay interference when the relay set Π_2 is selected.

3.2.2 The Second Relay Set Selection

Now let us turn to selecting the relay set Π_2 from the remaining $N - SK$ relay candidates, which operates in receive and transmit modes in even and odd time slots, respectively. After the selection of the relay set Π_1 , it is possible for the relay $\mathcal{R}_n \in \{1, \dots, N\} \setminus \Pi_1$ to compute the sum of inter-relay interference links generated by the relay set Π_1 , denoted by $\sum_{j=1}^K \sum_{t=1}^S |h_{n\pi_1(j,t)}^{(r)}|^2$, which can be estimated through pilot signaling sent from the relay nodes belonging to the relay set Π_1 . When the relay \mathcal{R}_n is assumed to serve the s th data stream of the k th S-D pair, it examines both i) how much interference is received from the undesired spatial beams created by RBF for the first hop and from the relay set Π_1 ; and ii) how much interference leakage is generated by itself to other destination nodes via OIA for the second hop. Then, the relay \mathcal{R}_n computes the following scheduling metric $L_{n,(k,s)}^{\Pi_2}$ termed *TIL* in this paper:

$$L_{n,(k,s)}^{\Pi_2} = L_{n,(k,s)}^{\Pi_1} + \sum_{j=1}^K \sum_{t=1}^S |h_{n\pi_1(j,t)}^{(r)}|^2, \quad (2)$$

where $n \in \{1, 2, \dots, N\}$ and $k \in \{1, 2, \dots, K\}$. As long as the relay nodes in the relay set Π_2 having a sufficiently small amount of the TIL are selected, the sum of inter-relay interference links received at the relay nodes in the relay set Π_1 becomes sufficiently small due to the channel reciprocity. As a result, our system is now capable of operating in *virtual full duplex* mode even with half-duplex relay nodes since the relay nodes in the relay set Π_1 are in receive mode with almost no inter-relay interference when the relay nodes in the relay set Π_2 are in transmit mode, or vice versa. In this selection stage, the relay set Π_2 is found in the sense of having negligibly small values of $L_{n,(k,s)}^{\Pi_2}$.

3.2.3 Implementation Based on Distributed Timers

After the two scheduling metrics $L_{n,(k,s)}^{\Pi_1}$ and $L_{n,(k,s)}^{\Pi_2}$ are computed at each relay node, a crucial question that we would like to raise is how to select relay nodes in a distributed manner. To answer this question, a timer-based method can be adopted similarly as in [34], [40], which operates based on the exchange of a short duration Clear to Send (CTS) message transmitted by each destination node who finds its desired relay node.⁵ Such a timer-based selection method

5. The reception of a CTS message that is transmitted from a certain destination node triggers the initial timing process at each relay node. Therefore, no explicit timing synchronization protocol is required among relay nodes [40]. Moreover, it is worth noting that the overhead of relay selection is a small fraction of one transmission block with small collision probability [40]. Note that our relay selection procedure is performed sequentially over all the S-D pairs and the selected relay node for a data stream of one certain S-D pair is not allowed to participate in the selection process for another data stream of the belonging S-D pair or another S-D pair.

would be considerably suitable in distributed systems in the sense that information exchange among relay nodes can be minimized. The selection process of the relay set Π_1 first begins. It is straightforward that the selection process of the relay set Π_2 can be performed in a similar manner.

(a) *The Selection Process of Π_1* . At the beginning of every scheduling period, the relay \mathcal{R}_n for $n \in \{1, 2, \dots, N\}$ computes SK scheduling metrics for all the data streams, consisting of S scheduling metrics $L_{n,(k,1)}^{\Pi_1}, \dots, L_{n,(k,S)}^{\Pi_1}$ for each source \mathcal{S}_k , where $k \in \{1, 2, \dots, K\}$. Then, the relay \mathcal{R}_n starts with SK timers whose initial values are proportional to the SK scheduling metrics. Thus, over the whole network, there are NSK timers prepared for the selection of Π_1 . Suppose that a timer of the relay $\mathcal{R}_{\pi_1(\hat{k},\hat{s})}$ having the smallest value in the network, denoted by $L_{\pi_1(\hat{k},\hat{s})}^{\Pi_1}$, expires first. Then, the relay $\mathcal{R}_{\pi_1(\hat{k},\hat{s})}$ transmits a short duration Ready to Send (RTS) message, signaling its presence, to other $N - 1$ relay nodes. The RTS message is composed of $\lceil \log_2 SK \rceil$ bits to indicate the corresponding data stream of a certain S-D pair to be served. Subsequently, the following actions are performed by relay nodes: i) the relay $\mathcal{R}_{\pi_1(\hat{k},\hat{s})}$ clears all its remained $SK - 1$ timers and keeps idle thereafter during the scheduling period; and ii) after receiving the RTS message sent by the relay $\mathcal{R}_{\pi_1(\hat{k},\hat{s})}$, other $N - 1$ relay nodes clear their timers corresponding to the data stream reserved by the relay $\mathcal{R}_{\pi_1(\hat{k},\hat{s})}$. Now, there exist $(N - 1)(SK - 1)$ timers left by $N - 1$ relay candidates. Each relay candidate continues to listen to the RTS message from other relay nodes while waiting for its own timer(s) to expire. If another relay node sends the second RTS message of $\lceil \log_2 (SK - 1) \rceil$ bits in order to declare its presence, then it is selected to communicate with the corresponding data stream of the S-D pair to be served. Each relay candidate keeps on checking the number of data streams reserved for each S-D pair. More precisely, if all S data streams of the k th S-D pair are reserved, then each relay candidate clears all its timers for the source \mathcal{S}_k . After SK RTS messages are sent out in consecutive order, yielding no RTS collision with high probability, the selection of Π_1 is terminated. When an RTS collision occurs (i.e., two or more relay nodes have exactly the same value of the scheduling metric), none of the relay nodes is selected. The network waits for such a relay node whose timer will expire next.

(b) *The Selection Process of Π_2* . The selection process of Π_2 begins after completion of selecting Π_1 . By changing the scheduling metric to $L_{n,(k,s)}^{\Pi_2}$, the set Π_2 can be selected from relay candidates $\mathcal{R}_n \in \{1, \dots, N\} \setminus \Pi_1$ by applying the distributed timer-based method as shown above. It is worth noting that for selection of the two relay sets Π_1 and Π_2 , only $2SK \lceil \log_2 SK \rceil$ bits could suffice for information exchange during the scheduling period, which would be negligibly small when L is large.

3.3 Data Transmission

After the selection process of two relay sets Π_1 and Π_2 , each source node (\mathcal{S}_k) starts to transmit S data streams to the corresponding destination node (\mathcal{D}_k) via S relay nodes belonging to either Π_1 or Π_2 . Without loss of generality, we focus on each odd time slot, i.e., $l_o = \{1, 3, \dots, L\}$. Let us first explain the basic operation of reception and transmission for the relay nodes in Π_1 . For the first hop, the relay nodes

$\mathcal{R}_{\pi_1(k,1)}, \dots, \mathcal{R}_{\pi_1(k,S)}$ in the relay set Π_1 receive the S spatial beams from the source \mathcal{S}_k , where each relay node is associated with one beam. The received signal $y_{\pi_1(k,s)}^{(1)}(l_o) \in \mathbb{C}$ at $\mathcal{R}_{\pi_1(k,s)}$ is given by

$$\begin{aligned} y_{\pi_1(k,s)}^{(1)}(l_o) &= \sum_{j=1}^K \sum_{t=1}^S \mathbf{v}_j^{(t)T} \mathbf{h}_{\pi_1(k,s)j}^{(1)} x_{j,t}^{(1)}(l_o) \\ &+ \sum_{j=1}^K \sum_{t=1}^S h_{\pi_1(k,s)\pi_2(j,t)}^{(r)} x_{\pi_2(j,t)}^{(2)}(l_o - 1) \\ &+ z_{\pi_1(k,s)}^{(1)}(l_o), \end{aligned} \quad (3)$$

where $z_{\pi_1(k,s)}^{(1)}(\cdot)$ is the complex additive white Gaussian noise (AWGN), which is i.i.d. over parameters s , k , and l_o , and has zero-mean and variance N_0 . For the second hop, the relay nodes in Π_1 forward the re-encoded symbols to the corresponding destination nodes by employing the DF relaying, where the received signal is fully decoded, buffered, and re-encoded, e.g., the relay node $\mathcal{R}_{\pi_1(k,s)}$ first recovers $x_{k,s}^{(1)}(l_o)$ in the slot l_o and forwards this signal to the destination node in the next slot l_o+1 .⁶ The received signal $\mathbf{y}_k^{(2)}(l_o+1) \in \mathbb{C}^{M \times 1}$ at the destination \mathcal{D}_k is given by

$$\mathbf{y}_k^{(2)}(l_o+1) = \sum_{j=1}^K \sum_{t=1}^S \mathbf{h}_{k\pi_1(j,t)}^{(2)} x_{\pi_1(j,t)}^{(2)}(l_o) + \mathbf{z}_k^{(2)}(l_o+1), \quad (4)$$

where $\mathbf{z}_k^{(2)}(\cdot) \in \mathbb{C}^{M \times 1}$ denotes the noise vector, each element of which is modeled by an i.i.d. complex AWGN random variable with zero-mean and variance N_0 .

Likewise, for the relay set Π_2 , the received signal at the relay $\mathcal{R}_{\pi_2(k,s)}$ for the first hop and the received signal at the destination \mathcal{D}_k for the second hop are given by

$$\begin{aligned} y_{\pi_2(k,s)}^{(1)}(l_o+1) &= \sum_{j=1}^K \sum_{t=1}^S \mathbf{v}_j^{(t)T} \mathbf{h}_{\pi_2(k,s)j}^{(1)} x_{j,t}^{(1)}(l_o+1) \\ &+ \sum_{j=1}^K \sum_{t=1}^S h_{\pi_2(k,s)\pi_1(j,t)}^{(r)} x_{\pi_1(j,t)}^{(2)}(l_o) \\ &+ z_{\pi_2(k,s)}^{(1)}(l_o+1), \end{aligned}$$

and

$$\mathbf{y}_k^{(2)}(l_o+2) = \sum_{j=1}^K \sum_{t=1}^S \mathbf{h}_{k\pi_2(j,t)}^{(2)} x_{\pi_2(j,t)}^{(2)}(l_o+1) + \mathbf{z}_k^{(2)}(l_o+2),$$

respectively.

At each time slot $l \in \{2, 3, \dots, L\}$, by employing OIA for the second hop, the resulting signal vector at the destination \mathcal{D}_k after post-processing is given by

$$\mathbf{r}_k(l) = [r_{k,1}(l), \dots, r_{k,S}(l)]^T \triangleq \mathbf{F}_k^H \mathbf{U}_k^H \mathbf{y}_k^{(2)}(l), \quad (5)$$

where $r_{k,s}(l) \in \mathbb{C}$ is the resulting signal corresponding to the s th data stream for $s \in \{1, 2, \dots, S\}$; \mathbf{U}_k indicates the null space of the interference space \mathbf{Q}_k (i.e., the signal space) at the destination \mathcal{D}_k and is multiplied so that inter-pair interference components are aligned to the interference

space at the destination \mathcal{D}_k ; and $\mathbf{F}_k \in \mathbb{C}^{S \times S}$ is a ZF equalizer expressed as

$$\begin{aligned} \mathbf{F}_k &= [\mathbf{f}_{k,1}, \dots, \mathbf{f}_{k,S}] \\ &\triangleq \left(\left[\mathbf{U}_k^H \mathbf{h}_{k\pi_b(k,1)}^{(2)}, \dots, \mathbf{U}_k^H \mathbf{h}_{k\pi_b(k,S)}^{(2)} \right]^{-1} \right)^H. \end{aligned}$$

Here, $\mathbf{f}_{k,s} \in \mathbb{C}^{S \times 1}$ for $s \in \{1, 2, \dots, S\}$ is the ZF column vector; and $b \in \{1, 2\}$ corresponds to the relay sets Π_1 and Π_2 , respectively.

4 ANALYSIS: DOF AND DECAYING RATE OF TIL

In this section, we shall analyze i) the DoF achieved by our proposed MS-OND protocol under a certain relay scaling condition and ii) the decaying rate of the TIL. The MS-OND protocol without alternate relaying and its achievable DoF are also shown for comparison.

4.1 DoF Analysis

In this section, using the scaling argument bridging between the number of relay nodes, N , and the received SNR (refer to [14], [15], [16] for the details), we show a lower bound on the DoF achieved by the MS-OND protocol in the multi-antenna $K \times N \times K$ channel with interfering relay nodes and the minimum N required to guarantee the DoF achievability.

The total number of DoF, denoted by $\text{DoF}_{\text{total}}$, is defined as

$$\text{DoF}_{\text{total}} = \sum_{k=1}^K \sum_{s=1}^S \lim_{\text{snr} \rightarrow \infty} \frac{T_{k,s}(\text{snr})}{\log \text{snr}},$$

where $T_{k,s}(\text{snr})$ is the transmission rate for the s th data stream of the source \mathcal{S}_k and $\text{snr} \triangleq \frac{P}{N_0}$. Under our MS-OND protocol where L transmission time slots per block are used, the achievable $\text{DoF}_{\text{total}}$ is lower-bounded by

$$\text{DoF}_{\text{total}} \geq \frac{L-1}{L} \sum_{k=1}^K \sum_{s=1}^S \sum_{b=1}^2 \left(\lim_{\text{snr} \rightarrow \infty} \frac{\frac{1}{2} \log(1 + \text{sinr}_{\min})}{\log \text{snr}} \right), \quad (6)$$

where $\text{sinr}_{\min} = \min(\text{sinr}_{\pi_b(k,s)}^{(1)}, \text{sinr}_{k,\pi_b(k,s)}^{(2)})$ is the minimum signal-to-interference-and-noise ratio (SINR) between the two hops. Here, $\text{sinr}_{\pi_b(k,s)}^{(1)}$ denotes the received SINR at the relay $\mathcal{R}_{\pi_b(k,s)}$ and $\text{sinr}_{k,\pi_b(k,s)}^{(2)}$ denotes the effective SINR for the s th stream at the destination \mathcal{D}_k , where $b = \{1, 2\}$ and $k \in \{1, 2, \dots, K\}$. More specifically, $\text{sinr}_{\pi_b(k,s)}^{(1)}$ can be expressed as

$$\text{sinr}_{\pi_b(k,s)}^{(1)} = \frac{P |\mathbf{v}_k^{(s)T} \mathbf{h}_{\pi_b(k,s)k}^{(1)}|^2}{N_0 + \mathcal{I}_{\text{IB}} + \mathcal{I}_{\text{IS}} + \mathcal{I}_{\text{IR}}},$$

where $\mathcal{I}_{\text{IB}} = P \sum_{t \neq s}^S |\mathbf{v}_k^{(t)T} \mathbf{h}_{\pi_b(k,t)k}^{(1)}|^2$ is the interference power caused by other generating beams of \mathcal{S}_k ; $\mathcal{I}_{\text{IS}} = P \sum_{j=1}^K \sum_{t=1}^S |\mathbf{v}_j^{(t)T} \mathbf{h}_{\pi_b(j,t)k}^{(1)}|^2$ is the interference power from other source nodes; and $\mathcal{I}_{\text{IR}} = P \sum_{j=1}^K \sum_{t=1}^S |h_{\pi_b(k,s)\pi_b(j,t)}^{(r)}|^2$ is the inter-relay interference. Let \tilde{b} denote the index of another relay set, resulting in $\tilde{b} = 2$ if $b = 1$ and vice versa. From (5), the received signal for the s th stream at \mathcal{D}_k , $r_{k,s}(l)$, is written as

6. We do not deal with buffering issues at the relay nodes because in our MS-OND protocol, each relay node needs only to buffer at most one data symbol.

$$r_{k,s}(l) = x_{\pi_b(k,s)}^{(2)}(l) + \sum_{\substack{j=1 \\ j \neq k}}^K \sum_{t=1}^S \mathbf{f}_{k,s}^H \mathbf{U}_k^H \mathbf{h}_{k\pi_b(j,t)}^{(2)} x_{\pi_b(j,t)}^{(2)}(l) + \mathbf{f}_{k,s}^H \hat{\mathbf{z}}_k(l), \quad (7)$$

where $\hat{\mathbf{z}}_k(l) \triangleq \mathbf{U}_k \mathbf{z}_k(l)$. From (7), $\text{sinr}_{k,\pi_b(k,s)}^{(2)}$ is given by

$$\text{sinr}_{k,\pi_b(k,s)}^{(2)} = \frac{P}{\|\mathbf{f}_{k,s}\|^2 N_0 + \sum_{\substack{j=1 \\ j \neq k}}^K \sum_{t=1}^S \left\| \mathbf{f}_{k,s}^H \mathbf{U}_k^H \mathbf{h}_{k\pi_b(j,t)}^{(2)} \right\|^2}.$$

We first focus on examining the received SINR values $\text{sinr}_{\pi_1(k,s)}^{(1)}$ and $\text{sinr}_{\pi_1(k,s)}^{(2)}$ according to each time slot in the perspective of relay set Π_1 . Let us define

$$\tilde{L}_{\pi_1(k,s),(k,s)} \triangleq L_{\pi_1(k,s),(k,s)}^{\Pi_1} + \sum_{j=1}^K \sum_{t=1}^S \left| h_{\pi_1(k,s)\pi_1(j,t)}^{(r)} \right|^2, \quad (8)$$

where $k \in \{1, 2, \dots, K\}$ and $s \in \{1, 2, \dots, S\}$. For the first hop (corresponding to the odd time slot l_o), the received $\text{sinr}_{\pi_1(k,s)}^{(1)}$ at $\mathcal{R}_{\pi_1(k,s)}^{(1)}$ is lower-bounded by

$$\begin{aligned} \text{sinr}_{\pi_1(k,s)}^{(1)} &\geq \frac{\text{snr} \left| \mathbf{v}_k^{(s)T} \mathbf{h}_{\pi_1(k,s)k}^{(1)} \right|^2}{1 + \text{snr} \left(L_{\pi_1(k,s),(k,s)}^{\Pi_1} + \sum_{j=1}^K \sum_{t=1}^S \left| h_{\pi_1(k,s)\pi_2(j,t)}^{(r)} \right|^2 \right)} \\ &= \frac{\text{snr} \left| \mathbf{v}_k^{(s)T} \mathbf{h}_{\pi_1(k,s)k}^{(1)} \right|^2}{1 + \text{snr} \tilde{L}_{\pi_1(k,s),(k,s)}} \\ &\geq \frac{\text{snr} \left| \mathbf{v}_k^{(s)T} \mathbf{h}_{\pi_1(k,s)k}^{(1)} \right|^2}{1 + \text{snr} \sum_{i=1}^K \sum_{t=1}^S \tilde{L}_{\pi_1(i,t),(i,t)}}, \end{aligned} \quad (9)$$

where the first inequality follows from (1) and (8). For the second hop (corresponding to the even time slot l_e), the effective $\text{sinr}_{k,\pi_1(k,s)}^{(2)}$ is lower-bounded by

$$\begin{aligned} \text{sinr}_{k,\pi_1(k,s)}^{(2)} &= \frac{\text{snr} / \|\mathbf{f}_{k,s}\|^2}{1 + \frac{\text{snr}}{\|\mathbf{f}_{k,s}\|^2} \sum_{\substack{j=1 \\ j \neq k}}^K \sum_{t=1}^S \left\| \mathbf{f}_{k,s}^H \mathbf{U}_k^H \mathbf{h}_{k\pi_1(j,t)}^{(2)} \right\|^2} \\ &\geq \frac{\text{snr} / \|\mathbf{f}_{k,s}\|^2}{1 + \text{snr} \sum_{\substack{j=1 \\ j \neq k}}^K \sum_{t=1}^S \left\| \mathbf{U}_k^H \mathbf{h}_{k\pi_1(j,t)}^{(2)} \right\|^2} \\ &\geq \frac{\text{snr} / \|\mathbf{f}_{k,s}\|^2}{1 + \text{snr} \sum_{t=1}^S L_{\pi_1(k,t),(k,t)}^{\Pi_1}} \\ &\geq \frac{\text{snr} / \|\mathbf{f}_{k,s}\|^2}{1 + \text{snr} \sum_{i=1}^K \sum_{t=1}^S L_{\pi_1(i,t),(i,t)}^{\Pi_1}} \\ &\geq \frac{\text{snr} / \|\mathbf{f}_{k,s}\|^2}{1 + \text{snr} \sum_{i=1}^K \sum_{t=1}^S \tilde{L}_{\pi_1(i,t),(i,t)}}, \end{aligned} \quad (10)$$

where the first inequality holds due to the Cauchy-Schwarz inequality. Here, the term $\sum_{i=1}^K \sum_{t=1}^S \tilde{L}_{\pi_1(i,t),(i,t)}$ in (9) and (10) needs to scale as snr^{-1} , i.e.,

$$\sum_{i=1}^K \sum_{t=1}^S \tilde{L}_{\pi_1(i,t),(i,t)} = O(\text{snr}^{-1}),$$

so that both $\text{sinr}_{\pi_1(k,s)}^{(1)}$ and $\text{sinr}_{k,\pi_1(k,s)}^{(2)}$ scale as $\Omega(\text{snr})$ with increasing snr , which eventually enables our MS-OND protocol to achieve the DoF of $\frac{L-1}{L}$ per stream from (6). Even if such a bounding technique in (9) and (10) may lead to a loose lower bound on the SINR, it is sufficient to prove our achievability result in terms of DoF and relay scaling laws.

Now, let us turn to the second relay set Π_2 . Similarly as in (9), for the first hop (corresponding to the even time slot l_e), the received $\text{sinr}_{\pi_2(k,s)}^{(1)}$ at $\mathcal{R}_{\pi_2(k,s)}^{(1)}$ is lower-bounded by

$$\text{sinr}_{\pi_2(k,s)}^{(1)} \geq \frac{\text{snr} \left| \mathbf{v}_k^{(s)T} \mathbf{h}_{\pi_2(k,s)k}^{(1)} \right|^2}{1 + \text{snr} \sum_{i=1}^K \sum_{t=1}^S L_{\pi_2(i,t),(i,t)}^{\Pi_2}},$$

where $L_{\pi_2(i,t),(i,t)}^{\Pi_2}$ indicates the TIL in (2) when $\mathcal{R}_{\pi_2(i,t)}^{(1)}$ is assumed to serve the t th data stream of the i th S-D pair. For the second hop (corresponding to the odd time slot l_o), the effective $\text{sinr}_{k,\pi_1(k,s)}^{(2)}$ is lower-bounded by

$$\text{sinr}_{k,\pi_2(k,s)}^{(2)} \geq \frac{\text{snr} / \|\mathbf{f}_{k,s}\|^2}{1 + \text{snr} \sum_{i=1}^K \sum_{t=1}^S L_{\pi_2(i,t),(i,t)}^{\Pi_2}}.$$

The next step is to characterize the three metrics $L_{j,(k,s)}^{\Pi_1}$, $L_{j,(k,s)}^{\Pi_2}$, and $\tilde{L}_{j,(k,s)}$ by computing their cumulative distribution functions (CDFs), where $j \in \{1, 2, \dots, N\}$, $k \in \{1, 2, \dots, K\}$, and $s \in \{1, 2, \dots, S\}$. The three metrics are used to analyze a lower bound on the DoF and the required relay scaling law in the model under consideration. Since it is obvious to show that the CDF of $\tilde{L}_{j,(k,s)}$ is identical to that of $L_{j,(k,s)}^{\Pi_2}$, we focus only on the characterization of $L_{j,(k,s)}^{\Pi_2}$. The scheduling metric $L_{j,(k,s)}^{\Pi_1}$ follows the chi-square distribution with $2(2SK - S - 1)$ degrees of freedom since it represents the sum of i.i.d. $2SK - S - 1$ chi-square random variables with 2 degrees of freedom each. Similarly, the TIL $L_{j,(k,s)}^{\Pi_2}$ follows the chi-square distribution with $2(3SK - S - 1)$ degrees of freedom. The CDFs of the two variables $L_{n,(k,s)}^{\Pi_1}$ and $L_{n,(k,s)}^{\Pi_2}$ are thus given by

$$\mathcal{F}_{L_1}(l) = \frac{\gamma(2SK - S - 1, l/2)}{\Gamma(2SK - S - 1)},$$

and

$$\mathcal{F}_{L_2}(l) = \frac{\gamma(3SK - S - 1, l/2)}{\Gamma(3SK - S - 1)},$$

respectively. Here, $\Gamma(z) = \int_0^\infty t^{z-1} e^{-t} dt$ is the Gamma function and $\gamma(z, x) = \int_0^x t^{z-1} e^{-t} dt$ is the lower incomplete Gamma function [41, eqn. (8.310.1)]. For further analytical tractability, we introduce the following lemma.

Lemma 1. For any $0 < l \leq 2$, the CDFs of the random variables $L_{n,(k,s)}^{\Pi_1}$ and $L_{n,(k,s)}^{\Pi_2}$ are lower-bounded by

$$\mathcal{F}_{L_1}(l) \geq C_1 l^{2SK-S-1}$$

and

$$\mathcal{F}_{L_2}(l) \geq C_2 l^{3SK-S-1},$$

respectively, where

$$C_1 = \frac{e^{-1} 2^{2SK-S-1}}{\Gamma(2SK - S - 1)}$$

and

$$C_2 = \frac{e^{-1} 2^{3SK-S-1}}{\Gamma(3SK-S-1)}. \quad (11)$$

Proof. The detailed proof is omitted here since it essentially follows the similar line to the proof of [14, Lemma 1] with a slight modification. \square

In the following theorem, we establish our first main result by deriving a lower bound on $\text{DoF}_{\text{total}}$ in the multi-antenna $K \times N \times K$ channel with interfering relay nodes.

Theorem 1. *Suppose that the MS-OND protocol with alternate relaying is used for the $K \times N \times K$ channel with interfering relay nodes when source and destination nodes are equipped with M antennas and each source node transmits S independent data streams. Then, for L data transmission time slots,*

$$\text{DoF}_{\text{total}} \geq \frac{L-1}{L} SK,$$

is achievable if $N = \omega(\text{snr}^{3SK-S-1})$.

Proof. A lower bound on the achievable $\text{DoF}_{\text{total}}$ is given by $\text{DoF}_{\text{total}} \geq \mathcal{P}_o \frac{L-1}{L} SK$, which reveals that $\frac{L-1}{L} SK$ DoF is achievable for a fraction \mathcal{P}_o of the time for actual transmission, where

$$\mathcal{P}_o = \lim_{\text{snr} \rightarrow \infty} \Pr \left\{ \text{snr} \sum_{k=1}^K \sum_{s=1}^S \tilde{L}_{\pi_1(k,s),(k,s)} \leq \epsilon_0 \right. \\ \left. \text{and } \text{snr} \sum_{k=1}^K \sum_{s=1}^S L_{\pi_2(k,s),(k,s)}^{\Pi_2} \leq \epsilon_0 \right\} \quad (12)$$

for a small $\epsilon_0 > 0$ independent of snr .

We now examine the relay scaling condition such that \mathcal{P}_o converges to one with high probability. For simplicity, suppose that Π_1 and Π_2 are selected out of two mutually exclusive relaying candidate sets \mathcal{N}_1 and \mathcal{N}_2 , respectively, i.e., $\mathcal{N}_1, \mathcal{N}_2 \subset \{1, 2, \dots, N\}$, $\mathcal{N}_1 \cap \mathcal{N}_2 = \emptyset$, $\mathcal{N}_1 \cup \mathcal{N}_2 = \{1, 2, \dots, N\}$, $\Pi_1 \subset \mathcal{N}_1$, and $\Pi_2 \subset \mathcal{N}_2$. Then, we are interested in examining how $|\mathcal{N}_1|$ and $|\mathcal{N}_2|$ scale with snr in order to guarantee that \mathcal{P}_o tends to approach one, where $|\mathcal{N}_b|$ denotes the cardinality of \mathcal{N}_b for $b = \{1, 2\}$. From (12), we further have

$$\mathcal{P}_o = \lim_{\text{snr} \rightarrow \infty} \left(\Pr \left\{ \text{snr} \sum_{k=1}^K \sum_{s=1}^S \tilde{L}_{\pi_1(k,s),(k,s)} \leq \epsilon_0 \right\} \right. \\ \left. \cdot \Pr \left\{ \text{snr} \sum_{k=1}^K \sum_{s=1}^S L_{\pi_2(k,s),(k,s)}^{\Pi_2} \leq \epsilon_0 \right\} \right). \quad (13)$$

Let $\mathcal{B}_{k,s}$ denote the set of the remaining relay candidates in the set \mathcal{N}_2 after the relay $\mathcal{R}_{\pi_2(k,s)}$ has been selected to deliver the s th stream of the k th S-D pair (note that $\mathcal{R}_{\pi_2(k,s)}$ belongs to Π_2), where the cardinality of $\mathcal{B}_{k,s}$ is denoted by $|\mathcal{B}_{k,s}|$. For a constant $\epsilon_0 > 0$ independent of snr , the second term in (13) can be lower-bounded by

$$\Pr \left\{ \sum_{k=1}^K \sum_{s=1}^S L_{\pi_2(k,s),(k,s)}^{\Pi_2} \leq \frac{\epsilon_0}{\text{snr}} \right\} \\ \geq 1 - \Pr \left\{ \max_{\substack{1 \leq k \leq K \\ 1 \leq s \leq S}} L_{\pi_2(k,s),(k,s)}^{\Pi_2} \leq \frac{\epsilon_0}{SK \text{snr}} \right\} \\ \geq 1 - \Pr \left\{ \exists k, s : L_{\pi_2(k,s),(k,s)}^{\Pi_2} \leq \frac{\epsilon_0}{SK \text{snr}} \right\} \\ \geq 1 - \sum_{k=1}^K \sum_{s=1}^S \Pr \left\{ L_{\pi_2(k,s),(k,s)}^{\Pi_2} \leq \frac{\epsilon_0}{SK \text{snr}} \right\} \quad (14) \\ \geq 1 - SK \Pr \left\{ \max_{j \in \mathcal{N}_2} L_{j,(k,s)}^{\Pi_2} \leq \frac{\epsilon_0}{SK \text{snr}} \right\} \\ \geq 1 - SK \left(1 - \mathcal{F}_L \left(\frac{\epsilon_0}{SK \text{snr}} \right) \right)^{|\mathcal{B}_{k,s}|} \\ \geq 1 - SK \left(1 - C_2 \left(\frac{\epsilon_0}{SK \text{snr}} \right)^{3SK-S-1} \right)^{|\mathcal{N}_2|-SK+1}.$$

We now turn to the first term in (13), which can be lower-bounded by

$$\Pr \left\{ \sum_{k=1}^K \sum_{s=1}^S \tilde{L}_{\pi_1(k,s),(k,s)} \leq \frac{\epsilon_0}{\text{snr}} \right\} \\ \geq 1 - \Pr \left\{ \max_{\substack{1 \leq k \leq K \\ 1 \leq s \leq S}} \tilde{L}_{\pi_1(k,s),(k,s)} \leq \frac{\epsilon_0}{SK \text{snr}} \right\} \quad (15) \\ = \left(\Pr \left\{ \tilde{L}_{\pi_1(k,s),(k,s)} \leq \frac{\epsilon_0}{SK \text{snr}} \right\} \right)^{SK},$$

where the equality holds due to the fact that $\tilde{L}_{\pi_1(k,s),(k,s)}$ and $\tilde{L}_{\pi_1(j,t),(j,t)}$ for $i \neq j$ or $s \neq t$ are functions of different random variables and thus are independent of each other. Let $K_{k,s} = \sum_{j=1}^K \sum_{t=1}^S |h_{\pi_1(k,s)\pi_2(j,t)}^{(r)}|^2$. From (9), we then have

$$\Pr \left\{ \tilde{L}_{\pi_1(k,s),(k,s)} \leq \frac{\epsilon_0}{SK \text{snr}} \right\} \\ = 1 - \Pr \left\{ L_{\pi_1(k,s),(k,s)}^{\Pi_1} + K_{k,s} \geq \frac{\epsilon_0}{SK \text{snr}} \right\} \quad (16) \\ \geq 1 - \Pr \left\{ L_{\pi_1(k,s),(k,s)}^{\Pi_1} \geq \frac{\epsilon_0}{2SK \text{snr}} \right\} \\ - \Pr \left\{ K_{k,s} \geq \frac{\epsilon_0}{2SK \text{snr}} \right\}.$$

In the same manner, let $\mathcal{A}_{k,s}$ denote the set of the remaining relay candidates in the set \mathcal{N}_1 after the relay $\mathcal{R}_{\pi_1(k,s)}$ has been selected to deliver the s th stream of the k th S-D pair (note that $\mathcal{R}_{\pi_1(k,s)}$ belongs to Π_1), and let $|\mathcal{A}_{k,s}|$ denote the cardinality of $\mathcal{A}_{k,s}$. Then, it follows that

$$1 - \Pr \left\{ L_{\pi_1(k,s),(k,s)}^{\Pi_1} \geq \frac{\epsilon_0}{2SK \text{snr}} \right\} \\ = 1 - \Pr \left\{ \min_{j \in \mathcal{N}_1} L_{j,(k,s)}^{\Pi_1} \geq \frac{\epsilon_0}{2SK \text{snr}} \right\} \quad (17) \\ = 1 - \left(1 - \mathcal{F}_L \left(\frac{\epsilon_0}{2SK \text{snr}} \right) \right)^{|\mathcal{A}_{k,s}|} \\ \geq 1 - \left(1 - C_1 \left(\frac{\epsilon_0}{2SK \text{snr}} \right)^{2SK-S-1} \right)^{|\mathcal{N}_1|-SK+1}.$$

From (14), (16), and (17), it is obvious that if $|\mathcal{N}_1|$ and $|\mathcal{N}_2|$ scale faster than $\text{snr}^{2SK-S-1}$ and $\text{snr}^{3SK-S-1}$, respectively, then

$$\lim_{\text{snr} \rightarrow \infty} \left(1 - C_1 \left(\frac{\epsilon_0}{2SK\text{snr}} \right)^{2SK-S-1} \right)^{|\mathcal{N}_1|-SK+1} = 0$$

$$\lim_{\text{snr} \rightarrow \infty} \left(1 - C_2 \left(\frac{\epsilon_0}{SK\text{snr}} \right)^{3SK-S-1} \right)^{|\mathcal{N}_2|-SK+1} = 0.$$

Under this condition, \mathcal{P}_o asymptotically approaches one, which means that DoF of $\frac{L-1}{L}SK$ is achievable with high probability if $N = |\mathcal{N}_1| + |\mathcal{N}_2| = \omega(\text{snr}^{3SK-S-1})$. This completes the proof. \square

Note that the achievable bound on $\text{DoF}_{\text{total}}$ asymptotically approaches SK for large L , which implies that our system operates in virtual full-duplex mode. The parameter N required to achieve SK DoF needs to increase exponentially with not only the number of S-D pairs, K , but also the number of data streams per S-D pair, S , so that the sum of $3SK - S - 1$ interference terms in the scheduling metric TIL in (2) does not scale with increasing snr at each relay node. Here, from the perspective of each relay node in Π_2 , the SNR exponent $3SK - S - 1$, indicating the total number of interference links, stems from the following three factors: i) the sum of interference power received from other spatial beams including not only the beams of other source nodes (i.e., $S(K-1)$ interfering links) but also other beams created by the same source node (i.e., $S-1$ interfering links); ii) the sum of interference power generating to other destination nodes (i.e., $S(K-1)$ interfering links); and iii) the sum of inter-relay interference power generated from Π_1 (i.e., SK interfering links). Thus, it is possible to enhance the achievable DoF in our MS-OND framework by increasing S (i.e., sending more data streams per S-D pair), at the cost of increased number of relay nodes.

Remark 1. SK DoF can be achieved by using the MS-OND protocol if N scales faster than $\text{snr}^{3SK-S-1}$ and the number of transmission slots in one block, L , is sufficiently large. In this case, all the interference signals are almost nulled out at each selected relay node via RBF for the first hop and are then almost aligned at each destination node via OIA for the second hop by exploiting the multiuser diversity gain. In other words, by applying the MS-OND protocol to the interference-limited multi-antenna $K \times N \times K$ channel such that the channel links are inherently coupled with each other, the links across each S-D path via $2S$ relay nodes can be completely decoupled with each other, thus enabling us to achieve the same DoF as in the interference-free channel case. We also note that deploying multiple antennas at relay nodes does not further increase the DoF in our system since the achievable DoF cannot go beyond MK and the MS-OND protocol has already achieved such DoF using a single antenna at each relay node. However, the multi-antenna configuration on the relay nodes would relieve the relay scaling condition required to achieve a target DoF owing to more effective interference management with multiple antennas.

Remark 2. We also show an upper bound on $\text{DoF}_{\text{total}}$ by using the cut-set bound argument similarly as in the single-antenna OND protocol [34, Section 4]. Suppose that \tilde{N} relay nodes are active, where $\tilde{N} \in \{1, 2, \dots, N\}$. Consider two cuts L_1 and L_2 dividing our network into two

parts in a different manner. Then, we can create an $MK \times (\tilde{N} + MK)$ MIMO channel under the cut L_1 . Similarly, an $(\tilde{N} + MK) \times MK$ MIMO channel is obtained under the cut L_2 . The DoF of the two MIMO channels is thus upper-bounded by MK . It turns out that our lower bound in Theorem 1 matches this upper bound for $S = M$ and large L .

4.2 Decaying Rate of TIL

In this section, we analyze the decaying rate of the TIL under the MS-OND protocol with alternate relaying, which can provide insights on how the TIL is bounded with increasing snr. It is found that the desired relay scaling law is closely related to the decaying rate of the TIL with respect to N for given snr.

Let $L_{SK\text{-th}}$ denote the TIL of the SK th selected relay node in time order (i.e., the last selected relay node). Thus, $L_{SK\text{-th}}$ is the largest one among all the SK TIL values of the selected relay nodes, which can be used to evaluate the interference controlling performance on the DoF. By Markov's inequality, a lower bound on the expectation of $L_{SK\text{-th}}$ with respect to N is given by

$$\mathbb{E} \left[\frac{1}{L_{SK\text{-th}}} \right] \geq \frac{1}{\epsilon} \Pr(L_{SK\text{-th}} \leq \epsilon),$$

where the inequality always holds for $\epsilon > 0$. Let $\mathcal{P}_{SK}(\epsilon)$ denote the probability that there exist only SK relay nodes among N relay candidates satisfying TIL $\leq \epsilon$, which is expressed as

$$\mathcal{P}_{SK}(\epsilon) = \binom{N}{SK} \mathcal{F}_L(\epsilon)^{SK} (1 - \mathcal{F}_L(\epsilon))^{N-SK}, \quad (18)$$

where $\mathcal{F}_L(\epsilon)$ is the CDF of the TIL. Since $\Pr(L_{SK\text{-th}} \leq \epsilon)$ is lower-bounded by $\Pr(L_{SK\text{-th}} \leq \epsilon) \geq \mathcal{P}_{SK}(\epsilon)$, a lower bound on the average decaying rate of the TIL is given by

$$\mathbb{E} \left[\frac{1}{L_{SK\text{-th}}} \right] \geq \frac{1}{\epsilon} \mathcal{P}_{SK}(\epsilon). \quad (19)$$

The next step is to find the parameter $\hat{\epsilon}$ that maximizes $\mathcal{P}_{SK}(\hat{\epsilon})$ with respect to ϵ in order to provide the tightest lower bound.

Lemma 2. When a constant $\hat{\epsilon}$ satisfies the condition $\mathcal{F}_L(\hat{\epsilon}) = \frac{SK}{N}$, $\mathcal{P}_{SK}(\hat{\epsilon})$ in (18) is maximized for a given N .

Proof. We refer to [34, Lemma 2] for the proof. \square

Now, we establish our second main theorem, which shows a lower bound on the decaying rate of the TIL with respect to N .

Theorem 2. Suppose that the MS-OND protocol with alternate relaying is used for the $K \times N \times K$ channel with interfering relay nodes when source and destination nodes are equipped with M antennas and each source node transmits S independent data streams. Then, the decaying rate of the TIL is lower-bounded by

$$\mathbb{E} \left[\frac{1}{L_{SK\text{-th}}} \right] \geq \Theta \left(N^{\frac{1}{3SK-S-1}} \right).$$

Proof. As shown in (19), the decaying rate of the TIL is lower-bounded by the maximum of $\frac{1}{\epsilon} \mathcal{P}_{SK}(\epsilon)$ over ϵ . By

Lemma 2, $\mathcal{P}_{SK}(\hat{\epsilon})$ is maximized when $\hat{\epsilon} = \mathcal{F}_L^{-1}\left(\frac{SK}{N}\right)$. Thus, we have

$$\begin{aligned} \mathbb{E}\left[\frac{1}{L_{SK-\text{th}}}\right] &\geq \frac{1}{\mathcal{F}_L^{-1}\left(\frac{SK}{N}\right)} \binom{N}{SK} \left(\frac{SK}{N}\right)^{SK} \left(1 - \frac{SK}{N}\right)^{N-SK} \\ &\geq \frac{1}{\mathcal{F}_L^{-1}\left(\frac{SK}{N}\right)} \left(\frac{N-SK+1}{N}\right)^{SK} \left(1 - \frac{SK}{N}\right)^{N-SK} \\ &\geq \frac{1}{\mathcal{F}_L^{-1}\left(\frac{SK}{N}\right)} \left(\frac{1}{SK}\right)^{SK} e^{-SK} \\ &\geq \Theta\left(N^{\frac{1}{3SK-S-1}}\right), \end{aligned}$$

where the second and third inequalities hold since $\binom{N}{SK} \geq \left(1 - \frac{SK}{N}\right)^{SK}$ and $\left(1 - \frac{SK}{N}\right)^{N-SK} \leq \left(1 - \frac{SK}{N}\right)^N \leq e^{-SK}$, respectively. By Lemma 1, it follows that $\frac{1}{\mathcal{F}_L^{-1}\left(\frac{SK}{N}\right)} \geq \left(\frac{C_2 N}{SK}\right)^{\frac{1}{3SK-S-1}}$, where C_2 is given by (11). Hence, the last inequality also holds, which completes the proof. \square

4.3 MS-OND Without Alternate Relaying

For comparison, the MS-OND protocol *without* alternate relaying is also described in this section. In the protocol, only the first relay set Π_1 participates in data reception and forwarding. In other words, the second relay set Π_2 does not need to be selected for the MS-OND protocol without alternate relaying. The overall procedure during one transmission block is described as follows.

(a) *Odd Time Slot* $l_o \in \{1, 3, \dots, L-1\}$. The K source nodes transmit their encoded symbols to the SK selected relay nodes in the set Π_1 . For instance, the source S_k transmits symbols $x_{k,1}^{(1)}(l_o), \dots, x_{k,S}^{(1)}(l_o)$ along with its S randomly generated spatial beams, where $k \in \{1, 2, \dots, K\}$. The relay $\mathcal{R}_{\pi_1(k,s)}$ receives the desired symbol $x_{k,s}^{(1)}(l_o)$ on the s th beam of S_k , where $s \in \{1, 2, \dots, S\}$.

(b) *Even Time Slot* $l_e \in \{2, 4, \dots, L\}$. The selected relay nodes in Π_1 forward their re-encoded symbols to the intended destination nodes. For instance, the relay nodes $\mathcal{R}_{\pi_1(k,1)}, \dots, \mathcal{R}_{\pi_1(k,S)}$ transmit their symbols $x_{\pi_1(k,1)}^{(2)}(l_e-1), \dots, x_{\pi_1(k,S)}^{(2)}(l_e-1)$ to the destination \mathcal{D}_k while the interfering signals to the other destination nodes are opportunistically aligned to their interference spaces. If the relay nodes in Π_1 successfully decode the corresponding symbols, then $x_{\pi_1(k,s)}^{(2)}(l_e-1)$ would be the same as $x_{k,s}^{(1)}(l_e-1)$.

When the relay \mathcal{R}_n is assumed to serve the s th beam of the k th S-D pair for $n \in \{1, 2, \dots, N\}$, $s \in \{1, 2, \dots, S\}$, and $k \in \{1, 2, \dots, K\}$, it computes the scheduling metric $L_{n,(k,s)}^{\Pi_1}$ in (1). With the computed $L_{n,(k,s)}^{\Pi_1}$, a timer based method is used for relay selection similarly as in Section 3.2.3. The DoF achieved by the MS-OND protocol without alternate relaying is shown in the following theorem.

Theorem 3. *Suppose that the MS-OND protocol without alternate relaying is used for the $K \times N \times K$ channel with interfering relay nodes when source and destination nodes are equipped with M antennas and each source node transmits S independent data streams. Then,*

$$\text{DoF}_{\text{total}} \geq \frac{SK}{2},$$

is achievable if $N = \omega(\text{snr}^{2SK-S-1})$.

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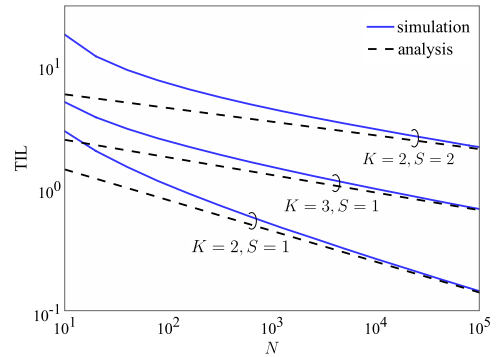


Fig. 2. The average TIL versus N for various K and S when the MS-OND protocol with alternate relaying is used in the multi-antenna $K \times N \times K$ channel with interfering relay nodes, where $M = 4$.

Proof. The detailed proof of this argument is omitted here since it basically follows the same line as the proof of Theorem 1. \square

Remark 3. On the one hand, it is observed from Theorem 3 that for *given* S (i.e., the fixed number of data streams per S-D pair), half of SK DoF can be achieved by the MS-OND protocol without alternate relaying under a less stringent relay scaling condition compared to the result in Theorem 1. For the MS-OND protocol with alternate relaying, in order to achieve the DoF of $\frac{L-1}{L}SK$, at least $\text{snr}^{3SK-S-1}$ relay nodes are required. For the MS-OND protocol without alternate relaying, in order to achieve the DoF of $\frac{SK}{2}$, at least $\text{snr}^{2SK-S-1}$ relay nodes are required. For instance, when $S = 1$, $K = 2$, and $\text{snr} = 5$ (in linear scale), $5^4 = 625$ relay nodes are necessary to achieve the DoF of almost 2 along with the MS-OND protocol with alternate relaying. Otherwise (i.e., when the number of relay nodes is less than the required number in practice), no DoF is guaranteed due to the inherent limitation of the opportunistic transmission mechanism. On the other hand, to achieve a *fixed target DoF*, the MS-OND protocol without alternate relaying requires more relay nodes when $K \geq 2$. For instance, suppose that the target DoF is $2K$. Then, the relay scaling condition required under the MS-OND protocol with alternate relaying is $\omega(\text{snr}^{6K-3})$, which is less stringent than another condition $\omega(\text{snr}^{8K-5})$ required under the MS-OND protocol without alternate relaying. This comes from the fact that to achieve $2K$ DoF, the MS-OND protocol without alternate relaying uses twice as many data streams. Moreover, it is seen that in a *finite N regime*, there exist snr regimes where the MS-OND protocol without alternate relaying outperforms that with alternate relaying in terms of sum-rates, which will be numerically verified in Section 5.

5 NUMERICAL EVALUATION

In this section, we perform computer simulations to validate our analytical results for finite N and snr . In our simulations, the channel coefficients in (3) and (4) are generated 1×10^5 times for each system configuration.

In Fig. 2, when the MS-OND protocol with alternate relaying is employed in the multi-antenna $K \times N \times K$ channel with interfering relay nodes, a log-log plot of the average TIL versus N is shown according to various parameter

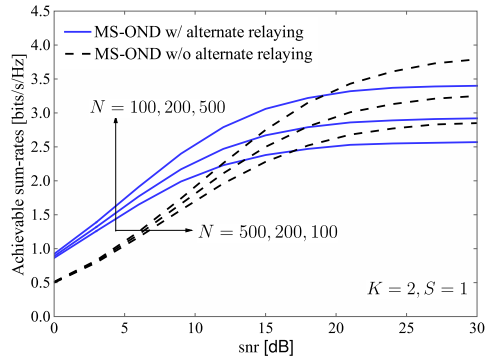
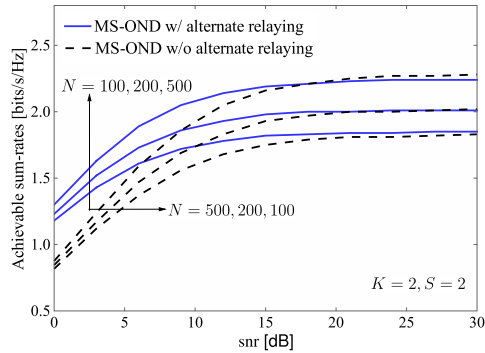
(a) $S = 1$.(b) $S = 2$.

Fig. 3. The achievable sum-rates versus snr, where $K = 2$, $M = 4$, and $N \in \{100, 200, 500\}$ in the multi-antenna $K \times N \times K$ channel with interfering relay nodes. The MS-OND protocols with and without alternate relaying are compared.

settings including $(K, S) = (2, 1)$, $(3, 1)$, and $(2, 2)$. The number of antennas at each S-D pair is set to $M = 4$ for all the simulations. It is numerically found that the TIL tends to linearly decrease with N for large N . It is further seen how many relay nodes are required to guarantee that the TIL is less than a certain small constant for given parameters K and S . In this figure, the dotted lines are also plotted from the theoretical result from Theorem 2 with a proper bias to check the slope of the TIL. We can see that the decaying rate of the TILs is consistent with the relay scaling law condition in Theorem 1. More specifically, the TIL is reduced as N increases with slopes of $\frac{1}{4}$ for $(K, S) = (2, 1)$, those of $\frac{1}{7}$ for $(K, S) = (3, 1)$, and those of $\frac{1}{9}$ for $(K, S) = (2, 2)$, respectively.

Fig. 3 illustrates the sum-rates achieved by the MS-OND protocols with and without alternate relaying in the $K \times N \times K$ channel with inter-relay interference versus snr (in dB scale), where $(K, S) = (2, 1)$ and $(2, 2)$, $N = \{100, 200, 500\}$, and $M = 4$. It is seen that in a finite N regime, there exists the case where the MS-OND protocol without alternate relaying outperforms the MS-OND protocol with alternate relaying. This is because for finite N , the achievable sum-rates for the alternate relaying case tend to approach a floor in a low or moderate SNR regime due to more residual interference in each dimension. The sum-rates for the MS-OND protocol without alternate relaying increase faster with snr in the low or moderate snr regime owing to less residual interference, compared to the MS-OND protocol with alternate relaying. However, the sum-rates achieved by both protocols tend to get saturated in the high snr regime because of more stringent relaying scaling condition

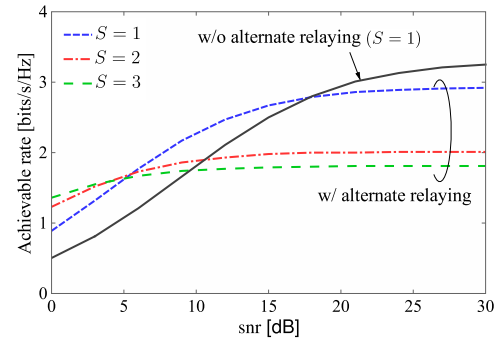


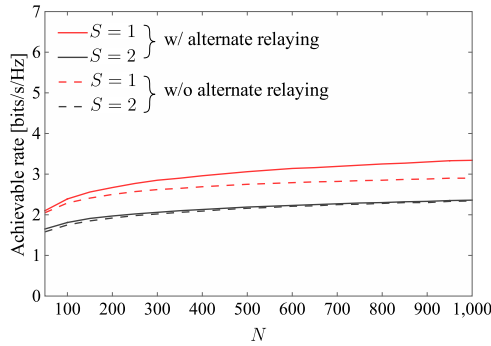
Fig. 4. The achievable sum-rates versus snr for various numbers of data streams per S-D pair, S , in the multi-antenna $K \times N \times K$ channel with interfering relay nodes, where $K = 2$, $M = 4$, and $N = 200$. The performance of MS-OND protocol without alternate relaying for $S = 1$ is also plotted.

for larger S (refer to Theorems 1 and 3). These observations motivate us to operate our system in switch mode where the relaying scheme is chosen between the MS-OND protocols with and without alternate relaying depending on not only the operating regime but also the system configuration.

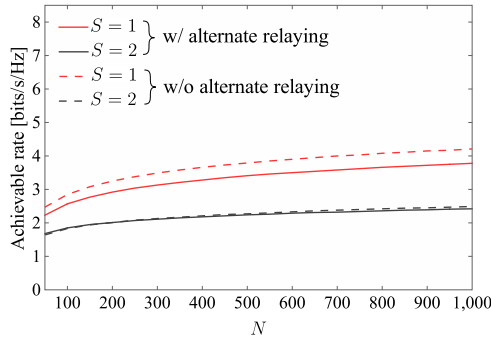
In Fig. 4, in order to examine which one is dominant between the MS-OND protocols with and without alternate relaying, the sum-rates achieved by both protocols in the $K \times N \times K$ channel versus snr (in dB scale) are plotted according to various S indicating the number of data streams per S-D pair, where $K = 2$, $M = 4$, and $N = 200$. It is seen that for the case with alternate relaying, large S leads to higher sum-rates in the low snr regime but gets saturated earlier. Thus, superior performance on the sum-rates can be achieved for small S in the high snr regime. It is also observed that the MS-OND protocol without alternate relaying for $S = 1$ outperforms all other cases with alternate relaying in the very high snr regime since it has the least stringent user scaling condition.

Fig. 5 illustrates the effect of the number of relay nodes, N , on the sum-rate performance for various S , where $K = 2$, $M = 4$, and $\text{snr} = \{15, 30\}$ [dB]. Owing to the opportunistic gain, it is obvious that the sum-rate increases with N for all cases. This observation implies that even if the relay scaling conditions in Theorems 1 and 3 are not fulfilled (in order to guarantee the target DoF), the sum-rate performance can still be enhanced with increasing N . For comparison of the two types of MS-OND protocols, it is found that the MS-OND protocol with alternate relaying outperforms its counterpart (i.e., the one without alternate relaying) when $\text{snr} = 15$ [dB], while the MS-OND protocol without alternate relaying achieves higher sum-rates than those of its counterpart when $\text{snr} = 30$ [dB]. This is due to the fact that according to Theorems 1 and 3, more stringent relay scaling condition is required in a higher snr regime, where the MS-OND protocol without alternate relaying relaxes the scaling requirement.

From the aforementioned observations, to achieve the maximum sum-rate, our system needs to operate in hybrid mode, which switches between the MS-OND protocols with and without alternate relaying and selects proper S depending on the operating regime. Table 2 is provided to demonstrate which strategy yields the highest sum-rate for different snr regimes according to various N by selecting one of four strategies I-IV indicated in the table, where we use "AR", "NAR", and T_{\max} to denote the MS-OND protocol



(a) snr = 15 [dB].



(b) snr = 30 [dB].

Fig. 5. The achievable sum-rates versus the number of relay nodes N in the multi-antenna $K \times N \times K$ channel with interfering relay nodes, where $K = 2$, $M = 4$, and $\text{snr} = \{15, 30\}$ [dB]. The MS-OND protocols with and without alternate relaying are compared.

with alternative relaying, the MS-OND protocol without alternative relaying, and the maximum sum-rate, respectively. From Table 2, the following interesting observations are made for each N : the strategy I tends to lead to the highest sum-rate in the very low snr regime; while the strategy IV tends to be dominant in the very high snr regime.

Furthermore, it would be meaningful to compare the performance of our protocol with another benchmark scheme in which single-antenna *full-duplex* relay nodes are deployed and SK relay nodes are opportunistically selected in the sense of generating or receiving the minimum sum of the interference from other spatial beams during the S-R transmission and the interference leakage to other destination nodes during the R-D transmission. Unlike our MS-OND protocol, such a full-duplex relaying protocol experiences not only the residual self-interference after SIC

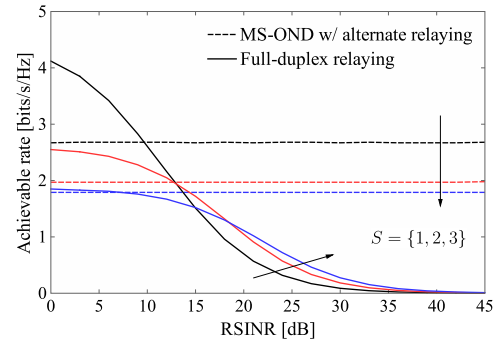


Fig. 6. The performance comparison between the full-duplex relaying scheme and the MS-OND protocol with alternate relaying in the multi-antenna $K \times N \times K$ channel with interfering relay nodes, where $\text{snr} = 15$ [dB], $N = 200$, $K = 2$, $M = 4$, and $S = \{1, 2, 3\}$. The performance of the MS-OND protocol with alternate relaying and the full-duplex relaying protocol is compared.

but also the full inter-relay interference, whereas it can achieve up to twice as much spectral efficiency as the half-duplex relaying case. Thus, it is not obvious which one is superior to another in the multi-antenna $K \times N \times K$ channel with interfering relay nodes. In Fig. 6, the sum-rates achieved by the MS-OND protocol with alternate relaying and the full-duplex relaying protocol in the $K \times N \times K$ channel versus residual self-interference-to-noise ratio (RSINR) (in dB scale) are plotted according to various S , where $\text{snr} = 15$ [dB], $N = 200$, $K = 2$, and $M = 4$. It is observed that there exists a crossover between two curves for a given S . Specifically, the full-duplex relaying protocol outperforms the MS-OND protocol in a low RSINR regime; but the sum-rates achieved by the full-duplex relaying protocol are significantly reduced with increasing RSINR. This implies that the advantage of full-duplex relaying is guaranteed only when powerful SIC can be implemented at the relay nodes, e.g., an RSINR lower than 10 dB is required for $S = 1$. Such a high requirement on the SIC would be quite stringent and challenging under mMTC or IoT networks consisting of low-cost relaying devices.

6 CONCLUSION

In this paper, we presented MS-OND to achieve the target DoF in the multi-antenna $K \times N \times K$ channel under a certain relay scaling law, where the source and destination nodes are equipped with M antennas while half-duplex relay nodes are equipped with a single antenna. The proposed MS-OND protocol that delivers S ($1 \leq S \leq M$) data

TABLE 2
The Lookup Table According to Operating Regimes

Strategy	I (AR, $S = 3$)	II (AR, $S = 2$)	III (AR, $S = 1$)	IV (NAR, $S = 1$)
$N = 50$	$\text{snr} \leq 4$ $T_{\max} \leq 1.42$	$4 < \text{snr} \leq 5$ $1.42 < T_{\max} \leq 1.45$	$5 < \text{snr} \leq 15$ $1.45 < T_{\max} \leq 2.09$	$15 < \text{snr}$ $2.09 < T_{\max}$
$N = 100$	$\text{snr} \leq 4$ $T_{\max} \leq 1.52$	$4 < \text{snr} \leq 5$ $1.52 < T_{\max} \leq 1.57$	$5 < \text{snr} \leq 16$ $1.57 < T_{\max} \leq 2.43$	$16 < \text{snr}$ $2.43 < T_{\max}$
$N = 200$	$\text{snr} \leq 3$ $T_{\max} \leq 1.55$	$3 < \text{snr} \leq 5$ $1.55 < T_{\max} \leq 1.67$	$5 < \text{snr} \leq 17$ $1.67 < T_{\max} \leq 2.77$	$17 < \text{snr}$ $2.77 < T_{\max}$
$N = 500$	$\text{snr} \leq 3$ $T_{\max} \leq 1.65$	$3 < \text{snr} \leq 5$ $1.65 < T_{\max} \leq 1.82$	$5 < \text{snr} \leq 19$ $1.82 < T_{\max} \leq 3.25$	$19 < \text{snr}$ $3.25 < T_{\max}$

streams per S–D pair was built upon the conventional OND in the single-antenna setup by leveraging both relay selection and interference management techniques. Two subsets of relay nodes among N relay candidates were opportunistically selected while alternate relaying was used in terms of generating or receiving the minimum TIL. For interference management, our protocol intelligently integrated RBF for the first hop and OIA for the second hop into the network decoupling framework. It was shown that our MS-OND protocol asymptotically achieves the optimal SK DoF, provided that the number of relay nodes scales faster than $\text{snr}^{3SK-S-1}$. Our analytical results were numerically validated through extensive computer simulations. Moreover, it was provided how the MS-OND protocol works in practice with a proper transmission and relaying strategy in finite N or snr regimes. Numerical evaluation showed that the strategy setting large S and adopting alternate relaying provides the best sum-rate performance in the low snr regime; on the contrary, the strategy setting $S = 1$ without alternate relaying outperforms all other cases in the very high snr regime. Hence, we shed light on the DoF-optimal design of distributed multi-stream transmission protocols based on partial channel knowledge in IoT or mMTC networks with a large number of sensors.

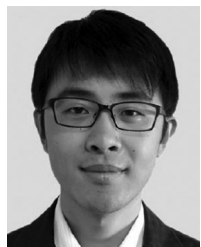
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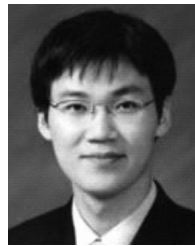
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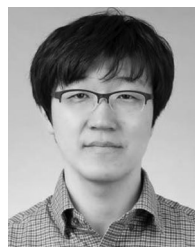
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